Platform Competition in Two-Sided Markets: The Case of Payment Networks

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Abstract

In this article, we construct a model to study competing payment networks, where networks offer differentiated products in terms of benefits to consumers and merchants. We study market equilibria for a variety of market structures: duopolistic competition and cartel, symmetric and asymmetric networks, and alternative assumptions about multihoming and consumer preferences. We find that competition unambiguously increases consumer and merchant welfare. We extend this analysis to competition among payment networks providing different payment instruments and find similar results.

JEL Classifications: D43, G21, L13

Key words: two-sided markets, payment systems, network externalities, imperfect competition

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1 Introduction

Two-sided markets are defined as a platform(s) providing goods and services to two distinct end-users where the platform attempts to set the price for each type of end-user to “get both sides on board” because the benefits of one type of end-user increases as the participation of the other type of end-user increases. Armstrong (2002), Evans (2003), and Rochet and Tirole (2003) suggest various examples of two-sided markets such as yellow pages (advertisers and users), adobe acrobat (creators of documents and readers), and television networks (viewers and advertisers). In this paper, we study an example of a two-sided market—payment networks (consumer and merchants).

Recently, antitrust authorities and courts in several jurisdictions have investigated the business practices of payment networks. In the United States, the Government sued MasterCard and Visa alleging anticompetitive business practices. The court ruled that MasterCard and Visa must allow financial institutions to issue competitor network credit cards such as American Express and Discover (see United States v. Visa U.S.A., Inc. (2001)). In another U.S. case that was settled out of court, around 5 million U.S. merchants sued the two card associations alleging an illegal tying of the associations offline debit cards and credit cards. The card associations agreed to unbundle their offline debit card branded product from their credit card branded product. In Australia, the Reserve Bank of Australia set rules for the determination of interchange fees, removed no-surcharge restrictions, and reduced barriers for entry to the market for credit card services (see Reserve Bank of Australia (2002)). The authorities in the European Commission and the United Kingdom have also investigated the business practices of the card associations (see European Commission (2002) and Cruickshank (2000)). These investigations has led to the development of several theoretical models to study pricing of payment services.

In this paper, we study the pricing strategies of payment networks that maximize the joint profits earned from both types of end-users. Recent investigations of these markets have focused on the determination of various prices including interchange fees, merchant discounts, and retail prices of goods and services within a single payment platform (see Chakravorti and Emmons (2003), Chakravorti and To (2003), Rochet and Tirole (2002), Schmalensee (2002), Schwartz and Vincent (2002), Wright (2003) and Wright (2004)).\(^1\) Often policy discussions have focused on whether each participant is paying her fair share of the underlying cost

\(^1\)For summary of these papers and others, see Chakravorti (2003).
Recently, Guthrie and Wright (2003) and Rochet and Tirole (2003) have investigated pricing decisions by payment networks when there are competing payment platforms. We build upon these two models by considering joint distributions for consumer and merchant benefits from participating on each network. In other words, each consumer and merchant is assigned a network-specific level of benefit from participating on each network. Consumers and merchants base their payment network usage decision on the difference between their individual network-specific benefit and that network’s participation fee. Our model also differs because we consider the effects of competition on price level and price structure. Unlike Guthrie and Wright, we consider fixed fees instead of per-transaction fees for consumers.\(^2\) We focus on the case where consumers choose to participate in only one payment network, often referred to in the literature as singlehoming, and merchants that are able to accept payment products from both networks, often referred to as multihoming. We consider three types of market structures for payment networks: cartel, non-cooperative duopoly under product differentiation, and Bertrand duopoly (price competition for homogeneous products). We find that competition unambiguously improves consumer and merchant welfare while reducing the profits of payment networks. Competition also affects the price structure. However, at a given price level, the price structure in a competitive duopoly may not be welfare-efficient.

### 2 Literature Review

While the literature on network effects is well established (see Farrell and Saloner (1985) and Katz and Shapiro (1985)), this literature ignores how to price services for two different sets of consumers where each set of consumer benefits from an increased level of participation by the other. Recently, several papers have investigated price structures in two-sided markets with network effects. Armstrong (2002), Caillaud and Jullien (2001), Jullien (2001), Rochet and Tirole (2003), and Schiff (2003) explore platform competition for various industries. A major contribution of this literature is that different types of consumers may not share equally in the costs of providing the good or service. In some cases, one-type of end-user may be subsidized. Many of the results depend on the accessibility of

\(^2\)Rochet and Tirole (2003) consider fixed fees as an extension of their model but restrict one side of the market to singlehome.
An example of a two-sided market with network effects is the market for payment services. Rochet and Tirole (2004) state that a necessary condition for two-sided markets is the failure of Coase theorem. A key observation in the market for payment services is that the law of one price generally prevails. In other words, merchants are reluctant to charge different prices based on the underlying cost of each payment instrument. The charging of one-price implies that there is not complete pass-through of the cost of payment instruments. However, Rochet and Tirole argue that the failure of Coase theorem is not sufficient for a market to be two-sided. They state that for a given price level, if the price structure affects the total volume of transactions on the platform, the market is said to be two-sided. Several models have shown that the interchange fee is not neutral under one-price policies and imperfect goods markets (Frankel (1998) and Gans and King (2003)).

Most of the payment network literature has only considered a single payment platform. Baxter (1983) models a four-party open network consisting of consumers, merchants, and their respective banks. Payment providers charge consumers and merchants usage fees. The merchant’s payment provider usually pays an interchange fee to the consumer’s payment provider. He finds that to balance the demands for payment services by consumers and merchants, an interchange fee may be required to compensate the financial institution that serves the group that benefits less and/or faces higher costs to bring that group on board. Rochet and Tirole (2002), Wright (2003), and Wright (2004) expand on Baxter by considering the effects of strategic interactions among payment system participants on the determination of the interchange fee.

Rochet and Tirole (2003) consider platform competition generally and investigate some characteristics of payment markets. First, they provide a general framework to model platform competition that is applicable to various markets. Second, they are able to characterize the determinants of price allocation between end-users. There may be instances where one end-user subsidizes the other. Third,

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3There is a long legal and regulatory history in the United States concerning the charging of different prices depending on the type of payment instrument used (see Chakravorti and Shah (2003)). Even in countries, where merchants face no restrictions to impose different prices, few merchants choose to do so (see IMA Market Development AB (2000) and Vis and Toth (2000)).

4There are also closed or proprietary networks where one entity serves all consumers and merchants that are members and operates the network. Examples of such networks include American Express and Discover in the United States.
they find that the seller’s price (could be viewed as the merchant discount in the payment services context) increases with captive buyers (buyers could be viewed as consumers in the payments context) and decreases when there are marquee buyers under certain conditions. Similarly, the buyer’s price moves in the opposite direction. Captive buyers prefer to use a certain platform and marquee buyers are coveted by sellers.

Guthrie and Wright (2003) also model competing payment networks where merchants use card acceptance as a strategic tool. They assume per-transaction costs for both consumers and merchants and each network’s benefit is identical to their competitors. Their main result is that when consumers hold only one card, competition between payment networks does not result in a lower interchange fee. However, if some consumers are able to hold more than one card, equilibrium interchange fees are lower if merchants are monopolists. If merchants compete for customers, merchants are willing to pay higher interchange fees potentially erasing any reduction in interchange fees.

Schiff (2003) explores platform competition in a Cournot duopoly, focusing on the effects of benefit asymmetry, for the two sides, on the market equilibria. He finds that multiple equilibria may occur for some parameter values. He also considers the possibility of having “open systems,” where subscribing to a network gives access to all agents on the other side of the market (independent of their network affiliations). In his framework, competing platforms have incentives to make their systems open.5

Our model differs from the existing literature in several ways. First, we focus on competing payment networks that offer payment instruments that have independent benefits and costs for consumers and merchants. In other models, consumers and merchants are indifferent between the benefits of each network. As a result, we are able to compare differences in consumer and merchant preferences to each network’s products. For example, certain consumers may prefer to pay with one network’s debit card while others may prefer to pay with another network’s debit card.6 Consumers may prefer one network’s product over another’s based on the types of services offered or the status of being a member. We also consider competition among different types payment instruments offered by different networks. Consumers not only choose among networks for a type of pay-

5This is equivalent to a special access regime (peering) used, especially, on the Internet. The economics of peering access is investigated in Little and Wright (2000), and Roson (2003).

6In the United States, there are two types of debit card networks—signature-based cards that use credit card networks to process transactions and PIN-based cards that use the ATM networks to process transactions. These types of transactions have different pricing structures.
ment instrument, but also choose among different types of payment instruments. We consider this case as an extension of our model.

Second, we consider the effects of competition on price level and price structure. Rochet and Tirole (2003) assume a small fixed level of profits for both issuing and acquiring sides in a non-profit joint-venture network. In reality, in both credit card and debit card markets, for-profit and non-profit networks co-exist. They consider welfare effects of changes in the price structure at a given price level. Similarly, Guthrie and Wright (2003) consider only welfare effects of changes in price structure and not of changes in the price level. In most of the model variants presented in these papers, networks maximize profits by maximizing the volume of transactions. This is important because, in many circumstances, social welfare maximization also implies maximizing the volume of transactions. In our model, maximizing profits is not generally the same as maximizing the volume of transactions, meaning that market prices are not necessarily welfare optimal.

Third, in our model, each network serves as both issuer and acquirer. Therefore, we do not explicitly model the interchange fee. However, we can implicitly consider interchange fees if there are differences in the demands of both types of end-users for the payment services and/or differences in costs to provide these services to the distinct type of end-users.

Fourth, in our model, consumers pay fixed membership fees and merchants pay per transaction fees. The introduction of fixed fees may restrict consumers from multihoming. We will explore the effects of this assumption below.

3 The Model

We construct a one-period model of payment network competition with three types of agents. There are two payment network operators. There are a large number of consumers \((C)\) and a large number of merchants \((M)\). Consumers demand one unit of each good and purchase goods from each merchant.

To focus on the choice of payment instrument, consumers and merchants derive utility based on the type of payment instrument used. There are three payment instruments. Cash is the default payment instrument available to all consumers and merchants at zero cost yielding zero utility for both consumers and merchants.⁷ There are two payment networks each offering a payment product that is associated with positive benefits for most consumers and merchants. These

⁷In reality, the cost of cash transactions is not zero and the utility of using cash is not zero. The
networks may offer similar products such as different types of credit cards or offer different types of instruments such as credit and debit cards. Each network provides services to both consumers and merchants directly and must recover the total cost of providing these services.

The total benefits, obtained by a consumer from being a member of a network, is given by a per-transaction benefit, \( h_i \), multiplied by the number of merchants accepting the payment product, \( D_i \). For each consumer, per-transaction benefits, \( h_i \), are independently distributed via a cumulative distribution with support \([0, \tau_i]\), where \( i \in \{1, 2\} \) is an index referring to the specific payment network. Consumer benefits may include convenience, extension of short-term and long-term credit, security, and status.

Unlike Rochet and Tirole (2003) and Guthrie and Wright (2003), we consider network benefits that are platform-specific. This is a key difference in our model. We motivate this difference by observing that different card networks provide different benefits to different consumers. For example, charge cards, instruments where consumers are not allowed to revolve balances, coexist with credit cards, instruments where consumers are allowed to revolve. The pricing structures differ between these two instruments as well. Charge cards such as American Express cards have traditionally charged higher fees than Visa and MasterCard cards where issuers earn revenue from finance charges to revolvers. Another example is the coexistence of signature-based and PIN-based debit cards where there are different price structures between these products. In our model, we allow some consumers to have strong preferences for a given network’s product and allow other consumers to have weaker preferences so that price structures may affect usage decisions.

Consumers pay an annual fee, \( f_i \), to access the payment system, allowing them to make an unlimited number of payments.\(^8\) While most U.S. issuers do not impose annual fees, some credit and debit card issuers that offer additional enhancements such as frequent-use awards impose annual fees. Generally, most European issuers impose annual fees.

We assume \( f_i \) is sufficiently high such that each consumer holds only one card.\(^9\) Utility from card holding is given by the difference between total bene-

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\(^8\)Guthrie and Wright (2003) do not consider fixed fees. Rochet and Tirole (2003) consider fixed fees as a special case of their model. The introduction of fixed fees does not allow for the consideration of multihoming consumers and merchants in an easily tractable model.

\(^9\)Given the marginal cost for card usage is zero and the marginal benefit is positive, consumers
fits from all transactions and the fee. Therefore, the total benefit to consumers increases as merchant acceptance increases. Once a consumer becomes a member of a payment network, we assume the consumer uses that network’s payment product exclusively with merchants that accept it. In other words, non-cash purchases dominate cash purchases for those consumers that are members of a payment network.

Each merchant is a monopolist selling an unique good.\textsuperscript{10} Merchant benefits could include security, convenience, and status. Merchants pay a per-transaction fee for each transaction, $f^m_i$, but cannot set different prices based on the payment instrument used.\textsuperscript{11} A payment type will be accepted whenever the per-transaction benefit $h^m_i$ (which is drawn randomly from a cumulative distribution function $F^m_i$, with support $[0, \mu_i]$) exceeds the per-transaction fee. Note that: (1) acceptance choices are independent, and (2) acceptance does not depend on the number of consumers that are members of that payment network whereas a consumer’s choice depends on the number of merchants accepting the payment card.\textsuperscript{12} There are three types of merchants. Those that accept neither of the payment network’s products because the benefit from accepting them is lower than the fee charged. Other merchants will only accept one of the payment network’s products because while the net benefit of one network is positive, the other is negative. Finally, some merchants will accept both non-cash payment products because there are positive benefits from doing so.

To sum up, utility for the representative consumer, $U^c$, and merchant, $U^m$, can be expressed as:

$$U^c = \max\{0, h_1^c D_1^m - f_1^c, h_2^c D_2^m - f_2^c\}$$  \hspace{1cm} (1)$$

$$U^m = \max\{0, D_1^c (h_1^m - f_1^m)\} + \max\{0, D_2^c (h_2^m - f_2^m)\}$$  \hspace{1cm} (2)$$

will prefer to use this instrument for all transactions. Similar arguments have been made for check usage in the United States, see Chakravorti and McHugh (2002).

\textsuperscript{10}Note that by construction, we ignore business stealing effects. Other models, such as Guthrie and Wright (2003), have shown that business stealing incentives may allow network operators to charge higher fees to merchants.

\textsuperscript{11}Pricing restrictions on merchants may take various forms. Non-discrimination pricing polices prohibit merchants from setting different prices based on the payment instrument used. In the United States, merchants are allowed to extend discounts for purchases made with non-credit card payment forms. However, card association rules usually prohibit surcharges for credit card purchases in most jurisdictions.

\textsuperscript{12}Clearly, if merchants are restricted to choosing only one payment network, the number of consumers that are members of a payment network would affect the merchants’ choice of networks.
where $D^c_i$ is the number of consumers holding network $i$’s instrument and $D^m_i$ is the number of merchants accepting network $i$’s product.  

Payment networks face two kinds of costs: a consumer fixed cost, $g_i$, and a merchant per-transaction cost, $c_i$. Networks maximize the following:

$$
\Pi_i = (f^c_i - g_i)D^c_i + (f^m_i - c_i)D^c_iD^m_i
$$

Networks choose simultaneously and non-cooperatively the consumer and merchant fees, taking the other network choices as given (a Nash equilibrium). Timing is as follows:

- Consumer and merchant benefits are randomly drawn;
- Networks maximize profits, by choosing $f^c_i$ and $f^m_i$;
- Merchants decide which payment forms to accept;
- Consumers decide which payment option to purchase;
- Transactions are realized.

The number of accepting merchants is determined, on the basis of the distribution function $F^m_i$:

$$
D^m_i = (1 - F^m_i(f^m_i))M
$$

Note that merchants accept non-cash payment alternatives as long as their benefits from doing so are greater than their costs. Because merchants only face per-transaction fees, they need only have one consumer using the network’s product to accept it as long as the benefit is greater than the cost.

The consumer side of the market is more complicated. To be chosen, a card has to pass two tests: (1) consumers must derive positive utility, and (2) the utility derived from this payment form must be higher than the other payment form. The market shares can be identified as in figure 1, where each consumer is mapped to a point, whose coordinates $(h^c_i D^c_i, h^m_i D^m_i)$ express total potential benefits from using card $i$ or $j$.

In figure 1, the large rectangle is divided into six parts. Consumers falling inside the smaller rectangle in the bottom left do not join either payment network.

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13Because we assume that consumers singlehome and always prefer to use non-cash payment alternatives, we equate membership in a payment network with usage of its product when merchants accept the payment product.
Figure 1: Network’s share of consumers
as their benefits are smaller than the membership fees of either network. Other consumers become members of either payment network $i$ if in rectangle $B$ or payment network $j$ if in rectangle $A$. When both networks are associated with positive utility, consumers choose on the basis of relative utility, and the border between the two market areas is given by the 45 degree segment that splits the square into triangles $C$ and $D$. Consumers in area $E$ also choose a network on the basis of relative utility, but their choice is primarily determined by the number of accepting merchants. For this reason, only the network offering the highest consumer surplus $(\tau D^m - f^c)$ attracts consumers in an area like $E$, which is absent if networks are symmetric and apply equal prices to both consumers and merchants.

Assuming uniform and independent random variables for consumer benefits for each payment product, the consumer demand for each network can be written as:

\[
D^c_i = \frac{(m_i - f^c_i) f^c_j + .5w^2 + (m_i - f^c_i - w)w}{m_im_j} C
\]

(5)

and

\[
D^c_j = \frac{(m_j - f^c_j) f^c_i + .5w^2 + (m_j - f^c_j - w)w}{m_im_j} C
\]

(6)

where:

\[
w = \min(m_i - f^c_i, m_j - f^c_j)
\]

\[
m_i = \tau_i m_i^m \quad m_j = \tau_j m_j^m
\]

**Profit Maximization**

When choosing the consumer and merchant fees, $f^c_i$ and $f^m_i$, each payment network maximizes profits, given by equation 3. It may be shown that optimal fees obey the following principle:

**Proposition 1** Profit maximizing fees can be determined on the basis of a “mod-
**ified Lerner rule**" that is:

\[ p^c + f^m - c = \frac{p^c}{\epsilon^c} = \frac{f^m}{\epsilon^m + \epsilon^m - \epsilon^m \epsilon^c} \]  

(7)

where \( p^c = \frac{f^c - g}{D^m} \) is the per-transaction revenue and cost from serving a consumer, and:

\[ \epsilon^c = \frac{\partial D^c}{\partial p^c} \frac{p^c}{f^m} \frac{1}{D^c} \]

\[ \epsilon^m = \frac{\partial D^m}{\partial f^m} \frac{f^m}{D^m} \]

\[ \epsilon_{cm} = \frac{\partial D^c}{\partial f^m} \frac{f^m}{D^m} \]

**Proof.** Following Rochet and Tirole (2003), substitute into equation 3, and consider the following problem:

\[
\max_{p^c, f^m} \log \Pi_i = \log (p^c_i + f^m_i - c_i) + \log D^c_i + \log D^m_i
\]  

(8)

Assuming log-concavity, equation 7 is obtained from simple manipulations of first-order conditions of the maximization problem 8, observing that:

\[
\frac{\partial p^c}{\partial f^m} = -\frac{f^c - g}{(D^m)^2} \frac{\partial D^m}{\partial f^m} = \frac{p^c}{f^m} \epsilon^m
\]

Proposition 1 highlights that the problem of setting optimal fees can be decomposed in two parts: the choice of the global price level \( p^c_i + f^m_i \), and the problem of balancing the relative prices \( p^c_i / f^m_i \).

When demand functions are expressed as in equations 4, 5, and 6, the distribution of merchant benefits is uniform in the interval \([0, \mu]\), and markets have both unitary mass, network elasticities are:

\[14\text{This result is an adaptation of a finding obtained by Rochet and Tirole (2003), who derive first order general conditions for profit maximization in a two-sided market. In deriving these conditions, however, they ignore the effect of a variation in network size on the price level. Equation 7 translates the result of Rochet and Tirole for our case, while taking into account the effect of network size on the consumer price. The result does not depend on specific assumptions about benefit distributions.}\]
The Effects of Competition on Prices and Welfare

To see how competition affects the market equilibrium, we now consider two cases: a duopoly, where each network maximizes its profits, assuming the competitor’s fees as given, and a monopoly, where an hypothetical cartel maximizes the sum of the two networks’ profits. The difference between the two cases is given by the fact that a monopolist internalizes any pecuniary externality, that is, any effect of a price change in the other operator’s profit. In other words, the cartel maximizes the sum of the two profit functions, as defined in equation 3.

Furthermore, as the following proposition states, pecuniary externalities have an unambiguous effect on the price level and welfare.

**Proposition 2** In the market for payment services defined above, the sum of consumer and merchant prices in duopoly are always lower than in monopoly, so that competition is always welfare enhancing for both consumers and merchants. Indeed, lower merchant fees increase merchant welfare and, indirectly, consumer welfare because of the higher number of accepting merchants. Lower consumer fees increase consumer welfare and, indirectly, merchant welfare because of the higher number of consumers in a network.

**Proof.** Since the number of of subscribing merchants is unaffected by the other network prices, cross-effects on profits only operate through changes in the consumers’ demand volume:

\[
\frac{\partial \Pi_i}{\partial f^c_j} = (f^c_i - g) \frac{\partial D^c_i}{\partial f^c_j} + (f^m_i - c) D^m_i \frac{\partial D^c_i}{\partial f^c_j} = \Pi_i \frac{\partial D^c_i}{D^c_i} \frac{\partial D^c_j}{\partial f^c_j} > 0
\]

\[
\frac{\partial \Pi_i}{\partial f^m_j} = (f^c_i - g) \frac{\partial D^c_i}{\partial f^m_j} + (f^m_i - c) D^m_i \frac{\partial D^c_i}{\partial f^m_j} = \Pi_i \frac{\partial D^c_i}{D^c_i} \frac{\partial D^m_j}{\partial f^m_j} > 0
\]
where the sign of both relationships is obtained from the definitions of utility 1 and 2.

An increase in both merchant and consumer fees applied by the competitor network expands the consumer demand. Consequently, the profit of a network increases if the competitor raises its prices. This is the conventional pecuniary externality due to competition. The perceived price elasticity of a competitive network will always be larger than that of a monopolistic cartel, and competition unambiguously reduces both merchant and consumer fees.

In the model with uniform and independent distributions for consumer and merchant benefits, cross price derivatives (and elasticities) are, in general, discontinuous, but they can be written in a compact way, using the notation introduced above:

\[
\frac{\partial D^c_i}{\partial f^c_j} = \frac{w}{m_i m_j} C > 0
\]

\[
\frac{\partial D^c_i}{\partial f^m_j} = \frac{\partial D^c_i}{\partial m_j} \frac{\partial m_j}{\partial f^m_j} = \left( \frac{m_i - f^c_i - w}{m_i m_j} - \frac{D^c_i}{m_j} \frac{\tau_j}{\mu_j} C M \right)
\]

\[
= \begin{cases} 
\frac{D^c_i \tau_j}{m_j \mu_j} C M > 0 & w = m_i - f^c_i \\
\frac{(m_i - f^c_i)^2}{2m_i (m_j)^2} \frac{\tau_j}{\mu_j} C M > 0 & w = m_j - f^c_j 
\end{cases}
\]

Proposition 2 has a simple intuitive explanation. A two-sided network has two instruments to attract more consumers: the prices applied to consumers and merchants. Both instruments, however, work to the same direction, expanding one network and reducing the competitor’s one. Despite the existence of two price instruments, pecuniary externalities work in the standard way.

This finding, intuitive as it may seem, is actually in sharp contrast with most recent literature on competition in credit card networks (e.g., Rochet and Tirole (2002), Guthrie and Wright (2003)), where it is shown that competition may be harmful for consumers and merchants. The key difference between our approach and the previous literature is that the latter is based on the (sometimes implicit) assumption of constant profits of the financial institutions of consumers and merchants and an often zero profit condition for the network itself.
If profits are constant for member banks, the main effect of competition is altering the price balance on the two market sides. However, as we show in the appendix, the equilibrium price structure is not generally welfare-efficient neither in competition nor in monopoly. In both cases, it would be possible to achieve higher aggregate welfare levels by reducing the price on one side, while increasing the price on the other side, so as to keep global network profits unchanged. The move from monopoly to competitive duopoly may not help in this sense. However, if profits are unconstrained, the overall price reduction dominates the effects on the price structure and welfare unambiguously improve for both sides.

It should be stressed that we retain the existence of two alternative platforms, even in the monopolistic setting. On the contrary, Schiff (2003) considers a monopoly with a single platform, finding that welfare may improve when switching from duopolistic competition to monopoly. Prices actually increase, but a single standard is imposed, which is beneficial in the presence of network externalities. This result may not hold in our model, however, because we consider network-specific preferences. Therefore, like in a monopolistic competition model, the trade-off between economies of scale and “taste for variety” should be taken into account.

**Symmetric Competition**

If networks are perfectly symmetric, equilibrium prices, in all market structures, must be equal. Guthrie and Wright (2003) consider some cases of symmetric competition between payment platforms. They focus solely on the price balance effect of competition, because they consider either a bank association with fixed margins on the two market sides, or proprietary schemes subject to Bertrand-like competition, dissipating profits. This implies that, in their model, total revenue is constant in all market structures.

In our model, market competition reduces total prices and increases merchant and consumer welfare. However, the price reduction is not, in general, uniform in the two sub-markets. To see this, consider the effects of a reduction in merchant and consumer fees on the other network’s demand volume. Figure 2 provides a graphical illustration of changes in market sizes generated by a reduction of consumer fee, whereas figure 3 provides a representation of the effects of a merchant fee reduction.

When the consumer fee is reduced in a network, the network’s demand expands because some new customers are convinced to choose this platform. Among these customers, some were not subscribing to any card before, whereas some others are now switching from the other network.
Figure 2: Market share effects of a reduction in a consumer fee
Figure 3: Market share effects of a reduction in a merchant fee
A reduction in a merchant fee, on the other hand, has an indirect effect on the other network demand. A reduction in the merchant fee affects the merchant’s demand, which in turn affects the consumer’s demand: $m$ shifts outward. The area corresponding to the competing network’s market share does not change, but the density of the consumers in the rectangle decreases.

Because of this “stretching effect” some consumers, previously associated with points slightly to the left of the 45 degree segment in figure 3, are now found to the right of this dividing line, in another market area.\footnote{Also, some previous non-subscribers, initially in the smaller lower left rectangle, are moved rightward into the market area.} These consumers are switching to the alternative network, not because consumer fees are lower there, but because there is a larger base of accepting merchants.

In a monopolistic two-sided market, a network operator selects prices to balance the two sides of the market (to get “both sides on board”). Under competition, the competitive pressure may be different in the two sub-markets, and the price structure, which emerges in equilibrium, depends on the different market conditions. In other words, competition does not simply drive the prices down, but also alters the balance of prices.

In our model, a key factor, determining the relative degree of competition between the two market sides, is given by:

$$\frac{\partial m}{\partial f^m} = -\frac{\tau M}{\mu}$$

that is, the factor translating a reduction in $f^m$ into an outward shifting of $m$.

We provide simulations of various equilibria to demonstrate relationships between different market structures. Table 1 presents parameter values, equilibrium fees, network profits, consumer and merchant demand, and total transaction volumes for a series of symmetric duopolistic and monopolistic market equilibria. The first four columns give parameter values: customer fixed costs, transaction costs, upper end of the merchant benefits distribution, upper end of the consumer benefits distribution. The parameters are not indexed, because they are identical for both networks. The subsequent four columns give equilibrium values for consumer and merchant fees, their difference, and equilibrium profits. The next three columns show each network’s demand volume for consumers and merchants and its total non-cash transactions.

Table 1A shows equilibrium values for each firm under duopolistic Nash competition and table 1B shows equilibrium values of each firm when the two firms...
operate as a cartel. The results show that for all parameter values the duopolistic competition results in lower consumer and merchant fees, higher consumer and merchant demand and a greater number of total transactions.

There are two cases where either the consumer fee or the merchant fee is zero (or even negative) in the duopolistic market. As expected from our previous discussion, this is a consequence of $\mu \ll \tau$, or $\mu \gg \tau$, making one side of the market significantly more competitive than the other.

Table 1: Symmetric Competition

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B: Cartel

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The fee for merchants does not significantly change in the two market structures. However, the fees to consumers changes drastically from the duopoly to

---

16The fourth and the fifth rows in table 1A show results for the same set of parameter values. In one case, consumers fee are constrained to be non-negative, whereas in the other case they can take negative values. There are examples of negative fees in the United States such as cashback programs. On the other hand, equilibrium fees in the cartel case are never negative. Also, it is easy to see that equilibrium merchant fees cannot be negative in any market structure.
the cartel. In column 7, we compute the difference between consumer fees and merchant fees, and we find that the difference increases for all parameter values.

The reason why consumers gain relatively more, in our examples, from market competition, is explained in the following proposition.

**Proposition 3** In the symmetric market with uniform and independent distributions of consumer and merchant benefits, there is more competitive pressure on the consumer side (higher marginal profits from a fee reduction) if, in the monopolistic equilibrium, either the merchant fee is zero, or:

\[
\frac{M f^c}{D^m} \leq 2\mu - \tau \tag{13}
\]

**Proof.** Assume \( f^m_j > 0 \). Starting from a symmetric equilibrium, suppose that either \( f^c_i \) or \( f^m_j \) are marginally decreased. In both cases, \( w = m_i - f^c_i \). Using this value for \( w \) in equations 11 and 12, we find that the marginal change in the consumer demand of the competing network, determining the pecuniary externality on profits (and the relative competitive pressure), is higher for the variation in consumer fees if:

\[
\left| \frac{\partial D^c}{\partial f^c_j} \right| \geq \left| \frac{\partial D^c}{\partial f^m_j} \right| \Rightarrow \frac{m - f^c}{m} \geq \frac{\tau M (m - f^c)[f^c + .5(m - f^c)]}{\mu m^2} \tag{14}
\]

where we dropped subscripts, for notational convenience, and we made use of the definition of demand 5 or 6. Condition 13 is obtained from simple manipulations of 14.

On the contrary, assume \( f^m_j = 0 \). In this case, the partial derivative of the consumer demand is discontinuous, because all merchants are already subscribing both networks, and a further reduction in the merchant fee would not bring about more merchants and, consequently, more consumers. The networks are therefore competing on one side only (the consumer one), and only consumer fees can decrease.

Observing that consumer fees cannot be negative in the cartel equilibrium, the following corollary can be immediately derived:\(^{17}\)

\(^{17}\)If \( f^c = 0 \) for both networks, all consumers subscribe to one network. Lower fees cannot increase total consumer demand or profits. On the other hand, negative fees can be observed in the competitive duopoly, because of the desire to undercut the competitor.
Corollary 1 A sufficient condition for the consumer fees falling less than merchant fees under competition, if merchant fees remain strictly positive, is:

\[ \tau \geq 2\mu \]  

What is the meaning of \( \tau \) and \( \mu \)? They are both parameters determining the amplitude of the interval of the (uniform) distribution function of transactional benefits for consumers (\( \tau \)) and merchants (\( \mu \)).

If the support of a distribution function is larger, there is more differentiation among agents. When \( \tau \geq 2\mu \) a marginal change in the consumer fee produces little effects on the consumer demand, but a marginal change in the merchant fee produces relatively large variations in the merchant demand. As a consequence, the duopolistic networks compete more vigorously on the merchant sub-market, and merchant fees decrease relatively more if condition 15 is met.\(^{18}\)

In the appendix, we look at the resulting price structures and see that they are not welfare efficient. Furthermore, although competition improves welfare because of a reduction in total price, the price structure may actually worsen in terms of welfare.

Asymmetric Competition
Most real markets involve competition between asymmetric players. For example, debit and credit cards are competing payment instruments, although they differ in terms of cost structure and services provided to consumers and merchants. Such competition has been investigated by the courts in the United States and by regulators in other parts of the world. We are not aware of any theoretical models that have attempted to investigate such competition.

Unfortunately, the analysis of asymmetric competition in the model illustrated above is very complex, and general analytical results cannot be readily obtained. Yet, useful insights can be gained through a combination of numerical examples and a careful inspection of the optimization condition 7, which still hold, in general, under asymmetry.

A simple way to address the issue is to start from a symmetric equilibrium and consider a marginal change in a specific cost or demand parameter, for one of the two networks. How will this perturbation of symmetry conditions affect the market equilibrium? This question can usefully be decomposed into two parts: (a) how will this change induce different aggregate price levels? (b) how will

\(^{18}\)In our numerical examples, this never occurs.
asymmetric conditions affect the balance between relative prices on the two sides of the market?

The first sub-question has a quite straightforward answer. The model considered here is reminiscent of an asymmetric Hotelling model, and results are similar. In an asymmetric Hotelling duopoly, consumers are evenly distributed along a [0,1] segment, with one firm located at point 0 and the other one located at point 1+\(\Delta\). Consumers buy one unit of a good, selecting the firm associated with the minimum total cost, which is the sum of producer price and transportation cost. In this case, it can be easily shown that (under full market coverage) prices applied by the first firm (and profits) are an increasing function of the parameter \(\Delta\), whereas the opposite occurs for the competitor. Analogously, in our model any cost increase, or any positive change in consumer/merchant preferences, will induce higher (aggregate) prices by a firm and a reaction by its competitor, which lowers its own (aggregate) prices.

In addition, the price balance between the two market sides also changes, because elasticities in equation 7 vary. Rochet and Tirole (2004) notice that this effect can be explained in the form of a simple “topsy-turvy principle”: a factor that is conducive to a high price on one side, to the extent that it raises the platform’s margin on that side, tends also to call for a low price on the other side, as attracting members on that other side becomes more profitable. Because the relevant cost concept in a two-sided market is the opportunity cost, any time an additional marginal unit is produced on one side, the network faces a marginal cost, but it can also raise the price on the other side, as the utility of the other side agents is increasing.

Coupling this effect with the asymmetric Hotelling one, we can see that any factor that is conducive to a high price on one side for one network induces: (a) a lower price on the other side for the same network, (b) a lower price on the same side for the other network, (c) a higher price on the other side for the other network. In other words, the networks follow a “reversed strategy” in terms of price balancing.

Table 2 presents equilibrium prices and demand volumes under asymmetric duopolistic competition and collusion, for a variety of parameter values. The cases could be interpreted as simulating (in a rather simplistic way) competition between a debit card network (network 2) and a credit card network (network 1). The latter is assumed to have higher customer costs and to provide more benefits to consumers (such as credit) and potentially, to merchants.

The effects of competition on the asymmetric market are not qualitatively different from the ones obtained under symmetry. This should not come as a surprise,
as the sign of pecuniary externalities in equations 11 and 12 were derived for the general case.

Numerical simulations confirm that relative prices, both in competition and in collusion, move in opposite directions, when parameter values for one network are changed from the symmetric benchmark. In all circumstances, when fees on one side of the market are lowered by a network, the other network reacts by lowering fees on the opposite market side.
### Table 2: Asymmetric Competition

#### A. Duopoly

**Network 1**

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<th>$\tau$</th>
<th>$f^c$</th>
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#### B. Cartel

**Network 1**

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4 Alternative Fee Structures and Assumptions

In this section, we consider alternative fee structures and assumptions and discuss how our results might be affected.

Reversed Multihoming
Consider the case where merchants pay fixed fees and consumers pay per-transaction fees. In the United States, some banks have started to charge per-transaction fees for online debit cards. Some observers of payment markets have suggested that the fixed fees associated with installing personal identification number pads may keep certain merchants from accepting them.

Given that consumers pay fixed fees and can only choose to be a member of one network, we found that consumers consider the number of merchants that accept a certain payment product in their decision to purchase payment services from that network. However, merchants only consider the net benefits of accepting cards for a single transaction because they multihome. Reversing who pays fixed fees and singlehomes and who pays per-transaction fees and multihomes, we would expect to see merchants choosing to accept payment cards based on the number of consumers that carry them and consumers choosing to hold both payment products because there is no cost in doing so.

In the United States, it is not uncommon to see consumers multihome among and across payment products. For credit cards, merchant acceptance of American Express and Discover credit cards is less than that of MasterCard and Visa cards. While consumers may prefer the former cards, they may carry the latter cards as insurance against merchants not accepting the former cards. Interestingly, most consumers multihome when it comes to signature-based and PIN-based debit cards, but merchants have started to reject certain types of debit cards and steer their customers to using a certain type of debit card.

Nonetheless, the results obtained from our model still hold, if the two market sides are switched. This can be easily done by re-interpreting all variables and parameters with a \( m \) superscript as referred to the consumers, and all variables and parameters with a \( c \) superscript as referred to the merchants.

\[ \text{For comparison, we are considering charge cards in this example. A substantial part of American Express cards are charge cards where consumers are not able to revolve. It is also noteworthy that American Express dominates the corporate card market suggesting that there are indeed strong consumer preferences.} \]
Endogenous Single/Multihoming

In the model presented in this paper, one side adopts a single platform (single-home) whereas the other one can use more than one platform (multihome). This configuration can emerge whenever the fixed cost of joining a network is sufficiently high, so that the cost of having a secondary payment instrument outweighs the potential benefits. This is, for example, the typical case of credit cards in most European countries, where consumers pay a fixed membership fee and typically carry only one card.

Ideally, as membership fee is endogenously determined within the model, so should be the single/multihoming decision. Endogeneizing this choice, however, can easily make the model analytically intractable. To our knowledge, only one paper (Hermalin and Katz (2004)) has addressed the issue of bilateral multihoming, through extensive use of numerical simulations.

Furthermore, new issues arise. For example, if both sides have both instruments available, who decides which platform will be used? Can one side refuse to accept or to adopt one instrument, only to steer the other side to the most preferred alternative? Clearly, these are all interesting issues, whose investigation falls, however, outside the scope of this paper.

Bertrand-like Competition

Instead of assuming that benefits are independently drawn for each payment network, consider the opposite polar case of perfect correlation. For example, a consumer may value the possibility of making credit card transactions, irrespective of the type of card. Yet, cards may be qualitatively differentiated. Basic benefits are the same for the two payment instruments, although they are consumer-specific.

This case can be accommodated by assuming that a uniform random variable \( x \) in the interval \([0, 1]\) is drawn for each consumer, and basic benefits are obtained by multiplying this variable by (network-specific) maximum basic benefits \( \tau_i \). In this case:

\[
U^c = \max \{0, x\tau_1 D^m_1 - f^c_1, x\tau_2 D^m_2 - f^c_2\} \tag{16}
\]

Again, to be chosen, a card must provide net benefits:

\[
x\tau_i D^m_i \geq f^c_i \Rightarrow x \geq \min \left(1, \frac{f^c_i}{\tau_i D^m_i}\right) \tag{17}
\]

and it must be better than the alternative one. Using the indifference condition:

\[
x\tau_i D^m_i - f^c_i = x\tau_j D^m_j - f^c_j \tag{18}
\]
we can define two sets, $[0, x]$ and $[x, 1]$, identifying the range of values of $x$, for which one network is preferred to the other.\(^{20}\)

The market share of a network is given by the intersection of this “preference set” and the set defined by equation 17. Of course, this intersection may be empty. There is one exception: when total maximum benefits and consumer fees are equal, the two market areas overlap and the consumer is indifferent between the two cards. In this case, we can assume that the market is equally split.

To understand how prices are set in a symmetric duopolistic equilibrium, start from arbitrary initial fee levels. On the consumer side, total demand would then be determined by the viability condition 17. From this point on, a slight reduction in the consumer fee or, equivalently, in the merchant fee, could allow each competitor to conquer the whole market (although total demand would change only marginally). That is, each competitor has an incentive to undercut either by lowering the consumer fee or by lowering the merchant fee.

The outcome is a special type of Bertrand price war with two instruments and the equilibrium is found when profits are dissipated. Each network tries to offer higher net benefits to the subscribing consumers. In equilibrium, consumer net benefits are maximized, under the constraint of non-negative profit for the networks.\(^{21}\)

This result is a direct consequence of the perfect correlation in the distribution of consumers’ benefits. In real markets, consumers are likely to have both ‘brand preferences’ and ‘payment tool preferences,’ irrespective of brand. In terms of Figure 1, consumers would then be located inside a positively sloped ‘cloud’ of points, and the market equilibrium would fall somewhere in between the two polar cases analyzed in this paper (perfect correlation vs. independent distributions of consumer benefits).

### 5 Policy Implications

Recently, pricing policies of credit card networks and debit card networks have been investigated by authorities in various jurisdictions. The apparent barriers to competition in the payment card industry and its harm to consumers and mer-

\(^{20}\) The implicit assumption here is $0 \leq x \leq 1$. Alternative cases are trivial.

\(^{21}\) A similar result is found by Guthrie and Wright (2003). In their model, however, consumers get their draw of transactional benefits after having subscribed a card. This implies that consumers are ex-ante equal, when making a subscription decision. However, Guthrie and Wright do not consider positive subscription fees.
chants has been the basis for investigations by the Reserve Bank of Australia, the U.S. courts along with authorities in other jurisdictions. However, few academic models address the issue of platform competition in the provision of payment services. As far as we aware, we are the first to consider competition among differentiated payment products being supplied by a single network or different networks. Our modelling strategy is justified by the coexistence of multiple payment networks that may serve various niche markets for a given payment instrument and/or supply multiple payment instruments.

In this paper, we address the effect of competing payment networks on consumer and merchant welfare. We find that competition unambiguously increases consumer and merchant welfare suggesting that policymakers should promote competition among networks providing similar products and those offering different products. Within a payment type such as credit cards, debit cards, or checks, providers offer various differentiated products. Our results suggest that not only are there benefits to competition within a payment type but also across payment types. Thus, when determining policies regarding payment networks, competitive pressures from similar and different payment products should be considered.

For an example of the effects of competition on price level, we look to the entry of credit cards in the U.S. grocery store market. In certain market segments, such as grocery stores in the United States, the acceptance of lower cost alternatives such as PIN-based debit cards resulted in lower merchant discounts for MasterCard and Visa branded credit cards. During the same time, there were no noticeable differences on the consumer side. In fact, certain card issuers are offering additional benefits to those cardholders that make purchases at grocery stores. To isolate the effect of competition on price structure is a bit more difficult. However, with the recent interchange fee regulation in Australia, some industry reports suggest that consumer benefits such as frequent-use enhancements will decrease because of lower interchange fees. Given that regulatory changes only recently took place, it is too early to tell the effect on the total volume of transactions.

We ignore some benefits of a single platform providing payment services or cooperation between payment networks. Payment services most likely exhibit

\[22\] For a discussion of competition among payment instruments, see Reserve Bank of Australia 2002. For a discussion of the recently settled merchant lawsuit against MasterCard and Visa, see Chakravorti (2003).

\[23\] Note that the benefits to grocers from credit cards may be less than other types of merchants. Some analysts have argued that some consumers may be reluctant to make food and other "necessary" good purchases on credit. For more details, see McAndrews and Stefanadis (1999).
economies of scale and scope.\textsuperscript{24} However, as noted above, consumers and merchants may have strong preferences for product differentiation resulting in potentially restricting scale economies. Some economists have argued that certain types of governance structures may limit monopoly rents. Hausman, Leonard, and Tirole (2003) suggest that if the payment platforms are not-for-profit entities and are not allowed to share profits with members, cooperation among the networks may limit the rents that could be earned. We leave these issues for future research.

6 Conclusion

To date most theoretical models consider a single platform with varying levels of competition among network participants. Few theoretical models have considered competing payment platforms. Unlike previous models, we consider network-specific benefits for consumers and merchants. We investigate the impact of competing payment networks on consumer and merchant welfare, network profits, and the ratio of consumer and merchant prices. We find that competition always improves consumer and merchant welfare. As expected, network profits decrease with competition. The ratio of consumer and merchant prices depend on the differences in the benefits.

However, we ignore some aspects of the payment industry captured by others. Most notably, we ignore strategic reasons for merchants to accept other payment products. Guthrie and Wright (2003) consider intratemporal business stealing as a motivation for merchants to accept payment cards. Business stealing would affect the level of merchant fees. However, the aggregate welfare of merchants does not improve with business stealing because net sales presumably remain constant. In fact, Chakravorti and To (2003) suggest that intertemporal business stealing may decrease merchant welfare under certain conditions.

In reality, consumers and merchants both multihome to some extent. Unfortunately, there are difficulties in modeling an environment where consumers and merchants both multihome in the presence of fixed fees. In markets such as the U.S. where consumers carry several payment products, consumers may still prefer to use one payment instrument for most transactions. Alternatively, consumers may have preferences for one payment instrument based on the value and type of the transaction. Therefore, consumers may carry more than one card as insurance

\textsuperscript{24}For discussion of scale and scope economies in payment services, see Chakravorti and Kobor (2003).
when one card is not accepted by the merchant or for some technical reason does not function. The underlying reasons why consumers multihome has not been modelled and remains a future direction of research.

In this paper, we extend the literature on payment networks that sheds light on the effects of competition on consumer and merchant welfare by considering a specific level of benefits for each consumer and merchant for each network’s payment services. We find threshold values when competition affects consumer prices or merchant prices more. While there are theoretical models that investigate network competition, these models have not been empirically tested. This type of empirical research is vital for policymakers to adopt the optimal polices regarding payment networks.
References


7 Appendix:
Sub-optimal Price Structures in Duopoly

In the paper, we showed that network competition unambiguously reduces equilibrium prices, and increases the number of subscribing merchants and consumers, as well as their welfare. However, neither monopoly nor competitive price structures are welfare-efficient. Furthermore, the introduction of market competition may not bring about better price structures, in terms of aggregate welfare of consumers and merchants. We show this for the symmetric case, using parameter values and prices of Table 1. Platform profits have been defined as:

$$\Pi = (f^c - g)D^c + (f^m - c)D^cD^m$$

Keeping the profit level fixed, a marginal change in the consumer fee would be compensated by a marginal change in the merchant fee if:

$$\frac{\delta f^c}{D^m} = -\delta f^m$$

Thus, we ask the following question: starting from any of the equilibria reported in Table 1, would it be possible to get a higher aggregate welfare for consumers and merchants, for the same level of platform profits?

To answer, we need first to identify the consumer and merchant welfare in the symmetric equilibria. For each single platform, aggregate consumer welfare ($CW$) and aggregate merchant welfare ($MW$) are given, in the symmetric case, by:

$$MW = \int_{f^c}^{\mu} (h - f^m)D^c dh$$

$$CW = \int_{0}^{f^c} \left( \int_{f^c}^{f^m} (h - f^c)dh \right) dk + \int_{f^c}^{m} \left( \int_{k}^{m} (h - f^c)dh \right) dk$$

where $m = \tau D^m$. This gives, under the assumption of uniform distribution:

$$CW = \frac{1}{(\tau D^m)^2} \left( \frac{(\tau D^m - f^c)^2 f^c}{2} + \frac{(\tau D^m - f^c)^3}{6} \right)$$

25Since we are considering a symmetric duopoly, total welfare can be easily computed by doubling the results.
To assess the welfare impact of a profit-neutral price rebalancing between the two market sides, we construct the following index:\textsuperscript{26}

\[
\eta = \left( \frac{\partial CW}{\partial f_c} + \frac{\partial MW}{\partial f_c} \right) D_m - \left( \frac{\partial CW}{\partial f_m} + \frac{\partial MW}{\partial f_m} \right)
\]

Therefore, a positive \( \eta \) means that it would be possible to get a higher aggregate welfare (consumer welfare + merchant welfare), by slightly augmenting \( f_c \), while reducing \( f_m \) so as to keep profits unchanged. The computation of \( \eta \) for parameter values and prices of Table 1 gives the following results for duopolistic competition (C) and monopolistic cartel (M):

<table>
<thead>
<tr>
<th>( q )</th>
<th>( c )</th>
<th>( \mu )</th>
<th>( \tau )</th>
<th>( \eta-C )</th>
<th>( \eta-M )</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>0</td>
<td>1</td>
<td>1</td>
<td>0.361</td>
<td>0.255</td>
</tr>
<tr>
<td>0</td>
<td>0.5</td>
<td>1</td>
<td>1</td>
<td>0.278</td>
<td>0.256</td>
</tr>
<tr>
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<td>1</td>
<td>1</td>
<td>0.265</td>
<td>0.221</td>
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<tr>
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<td>0</td>
<td>2</td>
<td>1</td>
<td>0.417</td>
<td>0.130</td>
</tr>
<tr>
<td>0</td>
<td>0</td>
<td>1</td>
<td>2</td>
<td>0.564</td>
<td>0.522</td>
</tr>
</tbody>
</table>

Notice that: (1) the \( \eta \) index is always positive, meaning that consumer fees are “too low”, and (2) introducing competition actually worsens the price structure. This is, of course, a direct consequence of the consumer fees falling relatively more in the competitive regime.

Summing up, market competition implies a downward pressure on prices, associated with a change in the price structure. The first effect is welfare-improving, whereas the second one may have negative welfare consequences. In our setting, the first effect dominates the second one, so that welfare of both consumers and merchants improves in any case.\textsuperscript{27}

\textsuperscript{26}Remember that, to keep profits unchanged, an increase (decrease) in \( f_m \) must be associated with a proportional decrease (increase) in \( f_c \), by a factor \( D_m \).

\textsuperscript{27}However, if we choose a different starting point, like a price-constrained monopoly, the second effect may be determinant, and competition may actually reduce welfare.