

Forces of Supply and Demand in a Soccer Player Market

Lesson by

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Lesson description

In this lesson, students will participate in an interactive market simulation. The market simulated is the labor market for professional soccer players in Europe. Students will play either the role of a team wishing to contract a player or a player looking for a team. The salary data generated from the simulation help students construct supply and demand curves in the market for players. Students will then discuss factors that could affect the market for professional players.

Concepts

Market	Labor market
Supply	Quantity supplied
Demand	Quantity demanded
Equilibrium salary	

Objectives

The student will be able to:

- 1. Define supply, demand, equilibrium price, market, and labor market.
- 2. Identify buyers and sellers in a simulated labor market.
- 3. Explain the role of economics in professional sports.
- 4. Graph a supply curve and a demand curve from simulation data.
- 5. Explain how a wage (price) acts as an incentive in a market.

6. Evaluate the extent to which a variety of factors impact wages in the market for professional soccer players in Europe.



Related content

Economics

Time required

90 minutes

Materials

- Visual 1: "What Does This List Represent?"
- Visual 2: "Record of Player Contracts"
- Visual 3: "Supply Schedule"
- Visual 4: "European Soccer Player Market Graph"
- Visual 5: "Demand Schedule"
- Handout 1: "Team Cards" (one copy, cut apart and ready to be distributed)
- Handout 2: "Player Information" (one per student)
- Handout 3: "Player Cards" (one copy, each card cut apart and ready to be distributed)
- Handout 4: "Team Information for Players" (one copy, cut apart and ready to be distributed to team representatives)
- Handout 5: "Supply and Demand Schedules" (one per student)
- Handout 6: "Graph" (one per student)

Method for displaying visuals

Note to instructor: The information in this lesson uses 2015 to 2016 season data. It is important to emphasize to the students the market is always changing and some players may have changed salaries or teams. The lesson can be used with the data provided even if it is no longer accurate. If you have students who are aware of the changes, discuss the conditions that caused the players to move and emphasize the role incentives played. If you are uncomfortable using the cards when they become inaccurate, please feel free to use the same data with fictional player names.

Procedures

Begin the lesson by displaying Visual 1: "What Does This List Represent?," Set 1. Ask the students what they
think the list represents and how the words on the list are related. When the correct answer is given, or after a
few minutes of guessing, display the label for Set 1 and the values of each team. Ask students whether or not
they were surprised by the top five teams on the list. Allow them to discuss for a minute or two.



- 2. Now display Visual 1: "What Does This List Represent?," Set 2. Ask the students what they think the new list represents and how the words on the list are related. When the correct answer is given, or after a few minutes of guessing, display the label for Set 2 and the average annual salary of each team. Ask students whether or not they were surprised by the top five teams on the list. Allow them to discuss for a minute or two.
- 3. Ask the students to identify the most common characteristic on both lists. The students will most likely answer with one of the following: "Real Madrid is second on both lists" or "Soccer teams top both lists."
- 4. Tell students that although soccer is not the main sport in the United States, it is the world's most popular sport to watch and to play. European soccer stars regularly top the charts as the world's most popular sports stars. Soccer is also the fastest-growing team sport in the United States. Tell students that it is with this in mind that the day's lesson will use information about the European soccer player market to learn about supply and demand.
- 5. Tell the students they will be divided into two groups. Twenty students will play the role of players. The remaining students will be representatives from six different professional soccer teams. If there are more than 26 students in the class, divide the remaining students evenly among the teams. If teams have more than one representative, they will be able to carry on more negotiations with players during the simulation.
- 6. Distribute Handout 1: "Team Cards" and Handout 2: "Player Information" to the team representatives. Be sure to point out the salary range and the maximum increase in salaries the team has established. Emphasize students cannot spend more than the amount listed on their card. Also, point out that they can use these funds to hire one player or several players. Their goal is to hire the best possible players at the best possible wage. Advise the team representatives to keep their salary maximum private during their negotiations with players. Tell them Handout 3 will give them a general overview of each player's strengths and weaknesses. Give students time to read the information before beginning the simulation.
- 7. Distribute Handout 3: "Player Cards" to each of the 20 students in the player group. The players should also receive a copy of Handout 2: "Player Information" and Handout 4: "Team Information for Players." Give the players time to read the information about themselves, the other players in the market, and the teams. Tell the players their goal is to negotiate a higher salary than their current salary. They should write their desired salary on their card.
- 8. Display Visual 2: "Record of Player Contracts." When students have finished reading their documents, tell them they are about to begin the simulation. Instruct the students to move around the room. Team representatives will call out the positions for which they are most interested in hiring. Players can call out their position and/or the salary they are willing to accept. As each team and player contract with each other, they will record the deal on their cards. Once hired, the player should go to the digital whiteboard and record the team and salary they chose on Visual 2. They should then have a seat and wait for the rest of the players to complete their negotiations.



- 9. Allow the negotiations to continue until there seems to be a slowing of activity. Tell students the market will be closing in two minutes. After two minutes, tell students to record their deal and have a seat. If any players were unable to negotiate a better salary, tell them to go to the salary chart and list their current team and salary.
- Tell players to calculate the percent change in their salaries. They should use the following formula: [(New Salary Old Salary)/Old Salary] X 100. Award a small prize to the player who negotiated the highest salary increase and a small prize to the player who negotiated the highest overall salary.
- 11. Ask the team representatives to calculate how much money (if any) they retained after hiring their players. Give a small prize to any team that was able to secure both of their desired players and had funds remaining.
- 12. Ask the students to share what factors seemed to influence their success or failure in the market. List these factors on the board as they share. Ask the students to discuss the similarities and differences they would expect between their classroom market for players and the real market for players.
- 13. Distribute Handout 5: "Supply and Demand Schedules" and Handout 6: "Graph." Students can fill in the supply and demand schedules and graph the schedules. Tell students they will now use their classroom market data to create supply and demand curves for the soccer player market.
- 14. Display Visual 3: "Supply Schedule." Beginning with the lowest wage negotiated, enter the supply curve information. Explain to students that the lowest-wage player was willing to offer his or her service very cheaply and becomes the first point on the supply curve. Enter the next lowest salary in the wage column. Tell the students that there are now TWO players willing to offer their services at the second wage. Since the first player was willing to accept the lower wage, it is logical to assume that player would also play for the higher wage. Explain that the number of players willing and able to supply their services at a particular wage is the quantity supplied. Continue this process until all 20 players have been added to the supply schedule. Have the students graph the supply schedule on their graph paper while you graph it on Visual 4: "European Soccer Player Market Graph."
- 15. Display Visual 5: "Demand Schedule." Beginning with the highest wage negotiated, enter the demand curve information. Explain to the students that only one team was willing to offer a very high wage for this player and becomes the first point on the demand curve. Enter the next highest salary in the wage column. Tell the students that there are now TWO teams willing to offer pay the second wage. Since the first team was willing to pay the higher wage, it is logical to assume this team would also demand the player at the second wage because it is lower than what it had to pay. Explain that the number of players teams are willing and able to demand at a particular wage is the quantity demanded. Continue this process until all 20 players have been added to the demand schedule. Have the students graph the demand schedule on their graph paper while you graph it on Visual 4: "European Soccer Player Market Graph."



- 16. After you and the students have graphed the demand and supply schedules, indicate the point at which the two lines cross. Ask the students what is special about this point. The students should respond that this point is where the quantity of players demanded is equal to the quantity of players supplied. (Be sure to correct their answer if they say supply equals demand. Explain that supply and demand refer to the whole curves, not just a point on the curve.) Tell students this point of intersection is known as equilibrium wage (or equilibrium price in a product market). It is the wage at which everyone who wants to work can find a position and everyone who wants to hire can find a player.
- 17. In conclusion, ask the students to write a five-sentence response on an exit card to the following prompt: What factors might influence a player's willingness and ability to supply his or her services at a particular wage and what factors might influence a team's willingness and ability to demand a player at a particular wage?

Sources: <u>www.espnfc.com</u>, <u>www.whoscored.com</u>, <u>http://bleacherreport.com/articles/1660422-europes-50-best-footballers-of-the-season/page/25</u>, <u>http://www.xe.com/currencyconverter/</u>



Visual 1: What Does This List Represent?

Set 1

Real Madrid

Dallas Cowboys

New York Yankees

Barcelona

Manchester United

Set 1

Top Five Highest-Valued Sports Teams in the World (2015)

Real Madrid \$3.26 billion

Dallas Cowboys \$3.20 billion

New York Yankees \$3.20 billion

Barcelona \$3.16 billion

Manchester United \$3.10 billion

Forbes 2015



Visual 1: What Does This List Represent? (Continued)

Set 2

Paris Saint-Germain

Real Madrid

Manchester City

Barcelona

Los Angeles Dodgers

Set 2

Top Five Teams with the Highest Average Annual Player Salaries

in the World (2015)

Paris Saint-Germain \$9,083,993

Real Madrid \$8,641,385

Manchester City \$8,597,844

Barcelona \$8,083,518

Los Angeles Dodgers \$8,023,207

Global Sports Salary Survey 2015



Visual 2: Record of Player Contracts

Player Name	Team Name	Salary
1. Maxime Gonalons		
2. Fernando Reges		
3. Michael Carrick		
4. Sergio Ramos		
5. Paul Pogba		
6. Bastian Schweinsteiger		
7. Gareth Bale		
8. Zlatan Ibrahimovic		
9. Juan Mata		
10. James Rodriguez		
11. Leo Messi		
12. Cristiano Ronaldo		
13. Roberto Firmino		
14. Andres Iniesta		
15. Phillip Lahm		
16. Manuel Neuer		
17. David De Gea		
18. Tim Howard		
19. Clint Dempsey		
20. Geoff Cameron		



Visual 3: Supply Schedule

Wage (Lowest to Highest)	Quantity of Players Supplied



Visual 4: European Soccer Player Market Graph





Visual 5: Demand Schedule

Wage (Highest to Lowest)	Quantity of Players Demanded



Handout 1: Team Cards

Γ	TEAM CARD						Γ	TEAM CARD					
			R	eal Madri (Spain)	d			Bayern Munich (Germany)					
A P C N C	Average Player Salary for Team:\$8,597,844Average Player Salary for League:\$1,857,36920Player Types Needed:Goalkeeper/MidfielderCurrent Salary Range:\$510,466.88 to\$21,695,731.20\$26,244,136.08Club Financial Info:\$26,244,136.08					A F C N	Average Player Salary for Team:\$7,660,968Average Player Salary for League:\$2,289,359Player Types Needed:Striker/DefenderCurrent Salary Range:\$58,938.10 to\$9,420,736.00\$60,650,000.00Club Financial Info:\$60,650,000.00				68 59 efender 10 to 36.00 000.00		
	Current Value	Per Cha in V sii Last	ange Value nce Year	Club Debt as a Percent of Overall Club Value	Annual Revenue	Annual Operating Income		Current Value Value Last Year		Club Debt as a Percent of Overall Club Value	Annual Revenue	Annual Operating Income	
	\$3.645 billion	+1	2%	3%	\$694 million	\$162 million		\$2.678 billion	+1	14%	0%	\$570 million	\$60 million
	Playe Signed	r d	Po	osition	Annual	Salary		Playe Signe	er d	Pc	osition	Annual	Salary
В	ased on 20	015–1	L6 data	1			E	Based on 2	015–2	16 data			



Handout 1: Team Cards (Continued)

TEAM CARD			TEAM CARD									
Juventus (Italy)	Juventus (Italy)							Paris Saint-Germain (France)				
Average Player Salary for Team:\$4,695,476Average Player Salary for League:\$3,350,430Player Types Needed:Striker/DefenderCurrent Salary Range:\$786,000 to\$7,873,240.82\$13,059,823.90Club Financial Info:\$13,059,823.90			A P C N	Average Player Salary for Team:\$9,083,993Average Player Salary for League:\$1,492,741Player Types Needed:Defender/ForvCurrent Salary Range:\$1,476,384.00\$15,503,124.0\$15,503,124.0Max Increase in Salary Spending:\$36,900,000Club Financial Info:\$36,900,000			93 41 r/Forward 84.00 to 124.00 000					
CurrentPercentClubCurrentChangeDebt as aValuein ValuePercentsinceofLast YearOverallClubValueClub	Annual Revenue	Annual Operating Income		Current Percent Cl Current Change Deb Value in Value Per since Cl Last Year Ove Va		Club Debt as a Percent of Overall Club Value	Annual Revenue	Annual Operating Income				
\$1.299 billion +55% 4%	\$390 million	\$81 million		\$814 million	2	8%	0%	\$588 million	\$1 million			
Player Position Signed	Annual	Salary		Playe Signe	r d	Pc	osition	Annual	Salary			
Based on 2015–16 data			E	Based on 2	015–:	16 data	1					



Handout 1: Team Cards (Continued)

Ī	TEAM CARD						<u> </u>	EAM CARD		
Å	AC Milan (Italy)						N (lewcastle (England)	è	
Average Player Salary for Team:\$4,085,126Average Player Salary for League:\$1,735,173Player Types Needed:Goalkeeper/DefenderCurrent Salary Range:\$176,000 to\$8,800,000.00\$8,800,000.00Max Increase in Salary Spending:\$46,500,000.00Club Financial Info:\$46,500,000.00				А Р С	Average Player Salary for Team:\$2,872,633Average Player Salary for League:\$3,822,003Player Types Needed:Midfielder/ForwCurrent Salary Range:\$322,888 to\$6,458,000\$6,458,000Max Increase in Salary Spending:\$34,000,000Club Financial Info:Sint Solary				33 03 er/Forward 5 to 00 000	
Current Value Last Year	Club Debt as a Percent of Overall Club Value	Annual Revenue	Annual Operating Income		Current Clu Current Change Debt Value in Value Perc since of Last Year Over Clu		Club Debt as a Percent of Overall Club Value	Annual Revenue	Annual Operating Income	
\$825 million +6%	32%	\$240 million	-\$29 million		\$383 million	+1	0%	0%	\$204 million	\$68 million
Player Po Signed	sition	Annual	Salary		Playe Signe	r d	Po	osition	Annual	Salary
Based on 2015–16 data				B	Based on 2	015–2	16 data	1		



Handout 2: Player Information

Maxime Gonalons, 27, midfielder	Leo Messi, 27, forward
Strengths: passing; wins ball in the air; clean tackles; ball	Strengths: one of the top players in the world; ball control;
interception	speed; avoiding defenders
Weaknesses: commits needless fouls; speed; free kicks	Weaknesses: shoots when he should pass to teammates
Fernando Reges, 28, midfielder	Cristiano Ronaldo, 31, forward
Strengths: on-field composure; pace of play; marking	Strengths: one of the top players in the world; pace of play; on
opponents; aerial ability; ball control	target shooting; crosses; ball control
Weaknesses: passing	Weaknesses: falls down too easily and too much; does tricks
	when he can easily just pass the ball
Michael Carrick, 34, midfielder	
Strengths: ball distribution; powerful shot; equally skilled with	Manuel Neuer, 31, goalkeeper
both feet; can play defensive or attacking midfield	Strengths: Shot stopping (Reflexes), Saving close range shots,
Weaknesses: on-target shots; unreliable performance, age	Saving long shots, Concentration
	Weaknesses: no significant weaknesses other than age
Sergio Ramos Garcia, 30, defender	
Strengths: versatility on the field; endurance; sustained	Andres Iniesta, 32, midfielder
attacking; finishing during set pieces	Strengths: technique; passing; endurance; consistency; ball
Weaknesses: on-field composure (gets red carded); difficulty	control; on-field composure; intelligence
refocusing after an attack	Weaknesses: size; strength
č	
Roberto Firmino, 24, forward	Paul Pogba, 23, midfielder
Strengths: excellent forward and goal scorer; great crossing;	Strengths: long shots; dribbling; aerial duels; key passes;
free-kick specialist	concentration
Weaknesses: struggles defending: has issues when confidence is	Weaknesses: passing ability
knocked	
	Devid De Cas. 25. geollegener
	David De Gea, 25, goalkeeper
Bastian Schweinsteiger, 31, midfielder	Strengths: consistently makes both easy and very difficult saves;
Bastian Schweinsteiger , 31, midfielder Strengths: pace of play; on-target shooting from right, left, and	Strengths: consistently makes both easy and very difficult saves; experience at many levels of play
Bastian Schweinsteiger , 31, midfielder Strengths: pace of play; on-target shooting from right, left, and center; set pieces	Strengths: consistently makes both easy and very difficult saves; experience at many levels of play Weaknesses: misses shots taken from long range; weak physical
Bastian Schweinsteiger , 31, midfielder Strengths: pace of play; on-target shooting from right, left, and center; set pieces Weaknesses: on-field composure	Strengths: consistently makes both easy and very difficult saves; experience at many levels of play Weaknesses: misses shots taken from long range; weak physical strength against opponents in the box
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Bastian Schweinsteiger, 31, midfielderStrengths: pace of play; on-target shooting from right, left, and center; set piecesWeaknesses: on-field composureGareth Bale, 26, attacking midfielderStrengths: on-target shots; free kicks; crossing the ball for assists Weaknesses: defenseZlatan Ibrahimovic, 34, forward Strengths: ball control; on-target shooting; agility Weaknesses: inconsistent focus; on-field composureJuan Mata, 28, midfielder Strengths: key passes; free kicks; speed; assists; set pieces Weaknesse: inconsistent focus; defense; tacklesJames Rodriquez, 24, midfielder Strengths: key passes; passing; finishing; free kicks Weaknesses: headers; aerial challengesPhillip Lahm, 32, defender Strengths: ball control; passing; consistent focus	 David De Gea, 23, goakeeper Strengths: consistently makes both easy and very difficult saves; experience at many levels of play Weaknesses: misses shots taken from long range; weak physical strength against opponents in the box Tim Howard, 37, goalkeeper Strengths: shot stops; blocking close-range shots Weaknesses: comes off his line; age; long passes; discipline Clint Dempsey, 33, forward Strengths: ball control; passing; setting up shots for teammates Weaknesses: physical strength, age Geoff Cameron, 30, defender Strengths: tackles; winning the ball in the air; on-field focus; ball control Weaknesses: sends too many long balls in the air; tackles too often; dribbles too long and loses the ball
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Handout 3: Player Cards

	PLAYE	R CARD				PLAYE	R CARD				
	Maxime	Gonald	ons		F	ernando (Fra	ancisc	o Reges	5)		
Age:	:	27			Age:		28				
Position:	I	Defensiv	e Midfiel	der	Position:		Defensiv	e Midfiel	der		
Team:	(Olympiq	jue Lyonn	ais (France)	Team:		Manche	ster City (England)		
Salary:	:	\$ 5,546,	667		Salary:	Salary: \$ 2,860,000					
Stats:					Stats:						
	Appearances	Goals	Assists			Appearances	Goals	Assists			
	32	0	0			24	2	0			
New Salary	Desired:	lary Accep	pted:	New Salary	Desired:	New Sa	lary Acce	oted:			
Team:Percent Change:					Team:		Percent	Change:			
Based on 20)15–16 data				Based on 20	15–16 data					
	PLAYF	R CARD				PLAYF	R CARD				
	Michae	I Carri	ck			Sergio Ra	mos G	arcia			
Age:	34				Age:	e e gre r ta	28				
Position:	Centra	al Midfi	elder		Position:		 Defende	er			
Team:	Manc	hester L	Inited (Er	ngland)	Team: Real Madrid (Spain)						
Salary:	\$ 6,11	0,894.4	0	0 /	Salary: \$ 12,870,000						
Stats:					Stats:						
	Appearances	Goals	Assists			Appearances	Goals	Assists			
	28	0	0			33	3	0			
New Salary	Desired:	New Sa	lary Accep	pted:	New Salary	Desired:	New Sa	lary Acce	oted:		
Team:		Percent	Change:		Team:		Percent	Change:			
Based on 20	15_16 data				Based on 20	15_16 data					
Based off 20	15 10 000				Dased off 20	15 10 4444					
	PLAYE	R CARD				PLAYE	R CARD				
	Roberto	Firmi	no			Bastian Sc	hweins	steiger			
Age:		24			Age:		31				
Position:	1	orward			Position:		Midfield	er			
Team:	L	iverpoo	I (England	1)	Team:		Manche	ster Unite	ed (England)		
Salary:	:	\$7,637,9	916.00		Salary:		\$20,982	2,318.50			
Stats:					Stats:						
	Appearances	Goals	Assists			Appearances	Goals	Assists			
	31	10	7			96	13	13			
New Colore	Desired			ata di	New Colore	Desired	New Ca		et e d		
New Salary	Desired:	New Sa		pied:	New Salary Desired: New Salary Accepted:						
		rercent	change:				Percent	Change:			
Based on 20	15-16 data				Based on 20	15-16 data					
based on 20	10 uald				based on 20	13-10 Uald					



Handout 3: Player Cards (Continued)

						PLAYER CARD					
	Garet	th Bale				Zlatan Ib	rahim	ovic			
Δσο·	Garci	26			Δσο·	210101110	rannin				
Position [.]		20 Attackin	a Midfield	ler	Position [.]	E0	rward				
Team [.]		Real Mar	drid (Snaii	n)	Team [.]	Pa	ris Saint	-Germain	e (France)		
Salary:		\$24 9 mi	llion	'/	Salary: \$36.4 million						
Stats:		72 1.3 mi	mon		Stats:						
	Appearances	Goals	Assists			Appearances	Goals	Assists			
	38	20	13			31	38	13			
New Salary	Desired:	New Sa	larv Accei	oted:	New Salary	Desired:	New Sa	larv Accei	oted:		
Team:		Percent	Change:		Team:		Percent	Change:			
		-					•	0.			
Based on 20	15–16 data				Based on 20	15–16 data					
	PLAYE	R CARD				PLAYE	R CARD				
	Juar	n Mata				James F	Rodria	uez			
Age:	• • • •	28			Age:		24				
Position:		 Attackin	g Midfield	der	Position:		Midfield	er			
Team:		Manche	ster Unite	ed (England)	Team:		Real Ma	drid <mark>(Spai</mark>	n)		
Salary:		\$11.5 m	illion	,	Salary:		\$21.4 m	illion	,		
Stats:					Stats:						
	Appearances	Goals	Assists			Appearances	Goals	Assists			
	38	6	35			32	8	10			
New Salary	Desired:	New Sa	lary Acce	pted:	New Salary	Desired:	New Sa	lary Acce	oted:		
Team:		Percent	Change:		Team:		Percent	Change:			
Based on 20	15–16 data				Based on 20	15–16 data					
	<u>PLAYE</u>	R CARD				PLAYE	R CARD				
	Leo	Messi				Cristiand	o Rona	ldo			
Age:		29			Age:	:	31				
Position:		Forward			Position:		Forward				
Team:		Barcelor	na (Spain)		Team:		Real Ma	drid (Spai	n)		
Salary:		\$48.5 m	illion		Salary:		\$52.2 m	illion			
Stats:					Stats:						
	Appearances	Goals	Assists			Appearances	Goals	Assists			
	48	41	21			47	51	15			
New Salary	Desired:	New Sal	lary Acce	nted.	New Salary	Desired:	New Sal	lary Acce	nted:		
Team:	Desired	Percent	Change		Team: Percent Change:						
		. creent	change.				rereent	change.			
Based on 20	15–16 data				Based on 2015–16 data						



Handout 3: Player Cards (Continued)

	PLAYER CARD	PLAYER CARD					
	Manuel Neuer	Andres Iniesta					
Age:	31	Age: 32					
Position:	Goalkeeper	Position: Midfielder					
Team:	Bayern Munich (Germany)	Team: Barcelona (Spain)					
Salary:	\$7,600,000	Salary: \$8,795,670					
Stats:		Stats:					
	Appearances Saves	Appearances Goals Assists					
	41 51	43 1 4					
New Salary Desi	red: New Salary Accepted:	New Salary Desired: New Salary Accepted:					
Team:	Percent Change:	Team:Percent Change:					
Based on 2015-1	l6 data	Pared on 2015, 16 data					
Dased 011 2013							
	PLAYER CARD	PLAYER CARD					
	Phillip Lahm	Paul Pogba					
Age:	30	Age: 23					
Position:	Defender	Position: Midfielder					
Team:	Bayern Munich (Germany)	Team: Manchester United (Engl	and)				
Salary:	\$9,384,128	Salary: \$5,072,805					
Stats:		Stats:					
Арр	pearances Goals Assists	Appearances Goals Assists					
	26 1 1	35 8 13					
New Salary Desi	red: New Salary Accepted:	New Salary Desired: New Salary Accepted:					
ream:	Percent Change:	Percent Change:					
Based on 2015–1	L6 data	Based on 2015–16 data					
	PLAYER CARD	<u>PLAYER CARD</u> Tim Llowerd					
A	David De Gea						
Age: Desition:	25 Coalkaapar	Age: 37					
Toom:	Manchester United (England)	Toom: Colorado Papids (USA)					
Salary:		Salary: \$2.6 million					
Stats:	413,273,02 4	Stats:					
	Appearances Saves	Appearances Saves					
	34 80	37 52					
New Salary Desi	red: New Salary Accepted:	New Salary Desired: New Salary Accepted:					
Team:	Percent Change:	Team:Percent Change:					
Based on 2015–1	L6 data	Based on 2015–16 data					



Handout 3: Player Cards (Continued)

	<u>PLAYE</u> Clint D	empse	ey		PLAYER CARD Geoff Cameron					
Age: Position: Team: Salary: Stats:	33 Forward Seattle Sounders (USA) \$3,913,008				Age: Position: Team: Salary: Stats:	29 Defender Stoke City (England) \$897,253				
	Appearances 30	Goals 12	Assists 10			Appearances 30	Goals 0	Assists 0		
New Salary Team: Based on 20	Desired:	New Sal	lary Acce t Change:	oted:	New Salary Team: Based on 20	Desired:	New Sa Percent	lary Acce Change:	oted:	



Handout 4: Team Information for Players (from <u>www.whoscored.com</u>)

Real Madrid		Bavern Munich											
Location: Madrid. Spain		Location: Munich, Germany											
,,													
League Rank:	2	League Rank: 1											
League Record (39 games):	26W-5L-7D	League Record (34 games): 29W-1L-4D											
Average Player Salary for To	eam: \$7,796,637	Average Player Salary for Team: \$5,907,652											
Real Madrid Characteristicso		Bayern Munich Characteristicso											
+ Strengths	- Weaknesses	+ Strengths											
Finishing scoring chances Very Strong Attacking set pieces Very Strong Counter attacks Very Strong Creating long shot opportunities Very Strong Creating chances using through balls Very Strong Creating scoring chances Very Strong Shooting from direct free kicks Very Strong Coming back from losing positions Strong Attrad duels Strong	Protecting the lead Stopping opponents from creating chances Avoiding offside Very V	ext Finishing scoring chances Very Strong Avoiding offside Weak ext Attacking down the wings Very Strong Stopping opponents from creating chances Weak ext Creating chances using through balls Very Strong Stopping opponents from creating chances Weak ext Creating chances through individual skill Very Strong Stopping opponents from creating chances Weak ext Defending set pieces Very Strong Creating scoring chances Strong Creating long shot opportunities Strong Creating set pieces Strong Attacking set pieces Strong Strong Strong											
Real Madrid Style		Coming back from losing positions Strong											
 Attempt through balls often Attack through the middle Control the game in the opposition's half Short passes Possession football Take a lot of shots Rotate their first eleven Opponents play aggressively against them Non-aggressive 		Bayern Munich Style Possession football Control the game in the opposition's half Attempt through balls often Short passes Non-aggressive Rotate their first eleven											
* Strengths, weaknesses and styles are calculated from team's cu	rrent domestic season statistics.	* Strengths, weaknesses and styles are calculated from team's current domestic season statistics.											
lunantus		Paris Osiat Osmasia											
		Paris Saint Germain											
Location: Turin, italy		Location: Pans, France											
League Rank:	1	League Rank: 1											
League Record (33 games):	- 22W-5L-6D	League Record (29 games): 30W-2L-6D											
Average Player Salary for To	am: \$4,695,476	Average Player Salary for Team: \$5,500,000											
	φ 1,000,170												
Juventus Characteristicso		+ Strengths - Weaknesses											
+ Strengths Shooting from direct free kicks Very Strong Creating long shot opportunities Very Strong Creating chances using through balls Very Strong Defending set pieces Very Strong Attacking set pieces Strong Juventus Style	- Weaknesses	Creating long shot opportunities Very Strong Creating chances using through balls Very Strong Creating chances through individual skill Strong Creating scoring chances Strong Finishing scoring chances Strong Protecting the lead Strong Stating the ball from the opposition Strong Defending set incres Strong											
Attempt through balls often													
 Possession tootball Attack through the middle 		Paris Saint Germain's Style of Play											
Control the game in the opposition's half		Attack through the middle											
Short passes		Short passes											
Von-aggressive		Attempt through balls often Possession football											
 Rotate their first eleven Opponents play aggressively against them 		X Take long shots											
* Strengths, weaknesses and styles are calculated from team's cur	ent domestic season statistics.	Non-aggressive Considerat first eleven											
		Consistent first eleven											



Handout 4: Team Information for Players (from <u>www.whoscored.com</u>)

AC Milan			Newcastle									
Location: Milan, Italy		Newcastle, England										
League Rank: League Record (24 games): Average Player Salary for Te	7 15W-11L-12D am: \$2,113,334		League Rank: League Record (24 gar Average Player Salary	nes): for Te	am:	16 6W-6L-4D \$2,239,808						
+ Strengths	- Weaknesses		Newcastle United Charact	eristics	0							
Counter attacks Very Strong Creating chances through individual skill Strong Attacking set pieces Strong Shooting from direct free kicks Strong Coming back from losing positions Strong Arial duels Strong Protecting the lead Strong	Stopping opponents from creating chances	Weak	+ Strengths Shooting from direct free kicks Creating chances using through balls Newcastle United Style	Strong Strong	 Finishing s Avoiding for Defending : Avoiding int Defending : Defending : Defending : 	- Weaknesses coring chances uling in dangerous areas against skillful players dividual errors set pieces against attacks down the wings	Weak Weak Weak Weak Weak Very Weak					
AC Milan's Style of Play Attacking down the right Possession football Opponents play aggressively against them Rotate their first eleven Aggressive			 Long balls Atempt <u>crosses</u> often Take a lot of shots Take long shots Play with width Playing in their own half Aggressive Play the offside trap Strengths, weaknesses and styles are calculated from 	m team's curre	ent domestic sease	on statistics.						



Handout 5: Supply and Demand Schedule

Supply Schedule

Wage (Lowest to Highest)	Quantity of Players Supplied

Demand Schedule

Wage (Highest to Lowest)	Quantity of Players Demanded



Handout 6: Graph

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